

How do we factor?

Multiply

$$(x+y)(x^2 - xy + y^2) = x^3 + y^3$$

~~$x^3 - xy + xy^2 + x^2y - xy^2 + y^3$~~

$$(x-y)(x^2 + xy + y^2)$$

$$x^3 + \cancel{y^3} = (x+\cancel{y})(x^2 - x\cancel{y} + \cancel{y^2})$$

$\downarrow$        $x+3)(x^2 - x(3) + 3^2)$

$$1) x^3 + 8$$

$$= x^3 + \cancel{2^3} = (x+2)(x^2 - x2 + 2^2)$$

$$\underline{(x+2)(x^2 - 2x + 4)}$$

1/4  
2/2

2)  $x^3 + 27$

$$= x^3 + \cancel{3^3} = (x+3)(x^2 - x(3) + 3^2)$$

$$= (x+3)(x^2 - 3x + 9)$$

Factor

$$\begin{aligned}
 & 27 + a^3 \\
 & = 3^3 + a^3 \\
 & = (3+a)(3^2 - 3a + a^2) \\
 & = (3+a)(9 - 3a + a^2)
 \end{aligned}$$

Factor

$$D^3 + D^3$$

$$\begin{aligned}
 & 8x^3 + 1 \\
 & = (2x)^3 + 1^3 \\
 & = (2x+1)((2x)^2 - 2x + 1^2) \\
 & = (2x+1)(4x^2 - 2x + 1)
 \end{aligned}$$

$$x^3 + y^3 = (x+y)(x^2 - xy + y^2)$$

$$(x-y)(x^2 + xy + y^2) = x^3 - y^3$$

$$= x^3 + \cancel{x^2y} + \cancel{xy^2} - \cancel{x^2y} - \cancel{xy^2} - y^3$$

$$x^3 - y^3 = (x-y)(x^2 + xy + y^2)$$

$$x^3 - 8 =$$

$$\begin{aligned} x^3 - 2^3 &= (x-2)(x^2 + x(2) + 2^2) \\ &= (x-2)(x^2 + 2x + 4) \end{aligned}$$